

10.2 Probability

What does it mean to say "something happens by chance"?

Describe an event that is IMPOSSIBLE. Describe an event that is CERTAIN.

probability - measures the likelihood that an event will occur, can be written as a fraction, decimal, or percent



Can you come up with an event with each of these probabilities?

| | | | | |
|-------------|-----------------|------------------------|--------------------|----------|
| 0% | 25% | 50% (equally likely) | 75% | 100% |
| pigs flying | winning lottery | flipping a coin: heads | the bell will ring | death !! |

Ex: There is a 80% chance of thunderstorms tomorrow. Describe the likelihood of the event.

LIKELY

Ex: The probability that you land a jump on a snowboard is $\frac{1}{2}$. Describe the likelihood of the event.

EQUALLY LIKELY

Ex: There is a 100% chance that the temperature will be less than 120°F tomorrow. Describe the likelihood of the event.

CERTAIN

Ex: There is a 20% chance of snow flurries tomorrow. Describe the likelihood of the event.

UNLIKELY

When all possible outcomes are equally likely, the probability of an event is:

$$P(\text{event}) = \frac{\text{number of favorable outcomes}}{\text{number of possible outcomes (total)}}$$

Examples of equally likely events: spinner (where all spaces are same size), bag of marbles (same # of each), coin, die/cube

Ex: You roll a number cube. Write out the outcomes (AKA sample space)

1, 2, 3, 4, 5, 6

- (a) What is the probability of rolling an odd number?

$$P(\text{odd \#}) = \frac{3}{6} = \frac{1}{2} = 0.5 = 50\%$$

- (b) What is the probability of rolling a number greater than 4?

$$P(\# > 4) = \frac{2}{6} = \frac{1}{3} = 0.\bar{3} = 33.\bar{3}\% = 33\frac{1}{3}\%$$

- (c) What is the probability of rolling an even number?

$$P(\text{even \#}) = \frac{3}{6} = \frac{1}{2} = 0.5 = 50\%$$

- (d) What is the probability of rolling a prime number?

$$P(\text{prime \#}) = \frac{3}{6} = \frac{1}{2} = 0.5 = 50\%$$

- (e) What is the probability of rolling a number greater than 2?

$$P(\# > 2) = \frac{4}{6} = \frac{2}{3} = 0.\bar{6} = 66.\bar{6}\% = 66\frac{2}{3}\%$$

- (f) What is the probability of rolling a number greater than 8?

$$P(\# > 8) = \frac{0}{6} = 0 = 0 = 0\%$$

Ex: The probability that you randomly draw a short straw from a group of 40 straws is $\frac{3}{20}$. How many are short straws? → equally likely

$$\frac{\text{short}}{\text{total}} = \frac{\text{short}}{\text{total}}$$

$$x = 3(2)$$

$$\frac{3 \xrightarrow{\times 2}}{20 \xrightarrow{\times 2}} = \frac{x}{40}$$

$$x = 6 \text{ short straws}$$

Ex: You randomly choose a paper clip from a jar that contains 6 green, 3 white, 4 red, 2 blue, 5 yellow. What is the probability of not choosing a green paper clip. Find the solution in 2 ways.

$$P(\text{not green}) = \frac{14}{20}$$

$$= \frac{7}{10} = 0.7 = 70\%$$

$$\begin{aligned} P(\text{not green}) &= 1 - \frac{6}{20} \\ &= \frac{20}{20} - \frac{6}{20} \\ &= \frac{14}{20} \end{aligned}$$